

**TABLA DE DERIVADAS**

$D(k) = 0$ donde $k = \text{constante}$
$D(k \cdot u) = k \cdot u'$
$D(u \cdot v) = u' \cdot v + v' \cdot u$
$D\left(\frac{u}{v}\right) = \frac{u' \cdot v - u \cdot v'}{v^2}$
$D(u^n) = n \cdot u^{n-1} \cdot u'$
$D(\ln u) = \frac{1}{u} \cdot u'$
$D(e^u) = e^u \cdot u'$
$D(a^u) = a^u \cdot u' \cdot \ln a$
$D(\operatorname{sen} u) = \operatorname{cos} u \cdot u'$
$D(\operatorname{cos} u) = -\operatorname{sen} u \cdot u'$
$D(\operatorname{tg} u) = \operatorname{sec}^2 u \cdot u'$
$D(\operatorname{cotg} u) = -\operatorname{cosec}^2 u \cdot u'$
$D(\operatorname{sec} u) = \operatorname{sec} u \cdot \operatorname{tg} u \cdot u'$
$D(\operatorname{cosec} u) = -\operatorname{cosec} u \cdot \operatorname{cotg} u \cdot u'$
$D(\operatorname{sh} u) = \operatorname{ch} u \cdot u'$
$D(\operatorname{ch} u) = \operatorname{sh} u \cdot u'$
$D(\operatorname{th} u) = \operatorname{sech} u \cdot u'$
$D(\operatorname{arctg} u) = \frac{1}{1+u^2} \cdot u'$
$D(\operatorname{argsh} u) = \frac{1}{\sqrt{1+u^2}} \cdot u'$
$D(\operatorname{argch} u) = \frac{1}{\sqrt{u^2-1}} \cdot u'$

**TABLA DE INTEGRALES**

$\int dx = x + c$
$\int x^m dx = \frac{x^{m+1}}{m+1} + c ; m \neq -1$
$\int \frac{dx}{x} = \ln x + c$
$\int e^x dx = e^x + c$
$\int a^x dx = \frac{a^x}{\ln a} + c$
$\int \operatorname{sen} x dx = -\operatorname{cos} x + c$
$\int \operatorname{cos} x dx = \operatorname{sen} x + c$
$\int \sec^2 x dx = \operatorname{tg} x + c$
$\int \operatorname{cosec}^2 x dx = -\operatorname{cotg} x + c$
$\int \operatorname{Sh} x dx = \operatorname{Ch} x + c$
$\int \operatorname{Ch} x dx = \operatorname{Sh} x + c$
$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \operatorname{arctg} \left( \frac{x}{a} \right) + c$
$\int \frac{dx}{a^2 - x^2} = \frac{1}{a} \operatorname{argth} \left( \frac{x}{a} \right) + c$
$\int \frac{dx}{\sqrt{a^2 - x^2}} = \operatorname{arcsen} \left( \frac{x}{a} \right) + c$
$\int \frac{dx}{\sqrt{x^2 - a^2}} = \operatorname{argCh} \left( \frac{x}{a} \right) + c$
$\int \frac{dx}{\sqrt{x^2 + a^2}} = \operatorname{argSh} \left( \frac{x}{a} \right) + c$

IDENTIDADES TRIGONOMETRICAS

1)  $\cos^2 u + \sin^2 u = 1$

2)  $\cos^2 u - \sin^2 u = \cos(2u)$

3)  $2 \cdot \sin u \cdot \cos u = \sin(2u)$

4)  $\text{Ch}^2 u - \text{Sh}^2 u = 1$

5)  $\text{Ch}^2 u + \text{Sh}^2 u = \text{Ch}(2u)$

6)  $2 \cdot \text{Sh} u \cdot \text{Ch} u = \text{Sh}(2u)$

7)  $\cos x = \cos^2 \frac{x}{2} - \sin^2 \frac{x}{2}$

8)  $\sin x = 2 \cdot \sin \frac{x}{2} \cdot \cos \frac{x}{2}$

Trabajando algebraicamente con estas identidades trigonométricas, podemos deducir lo siguiente:

De 1)  $\sin u = \sqrt{1 - \cos^2 u}$  y  $\cos u = \sqrt{1 - \sin^2 u}$

Sumando 1) + 2)  $\cos^2 u = \frac{1 + \cos(2u)}{2}$

Restando 1) - 2)  $\sin^2 u = \frac{1 - \cos(2u)}{2}$

De 4)  $\text{Ch} u = \sqrt{1 + \text{Sh}^2 u}$  y  $\text{Sh} u = \sqrt{\text{Ch}^2 u - 1}$

Sumando 4) + 5)  $\text{Ch}^2 u = \frac{1 + \text{Ch}(2u)}{2}$

Restando 4) - 5)  $\text{Sh}^2 u = \frac{\text{Ch}(2u) - 1}{2}$